

A New Bubble point Pressure Correlation of Egyptian Crude Oils

Ramadan Emara^{1,2}

(Home) Al Azhar University, Faculty of Engineering, Mining and Petroleum Engineering Department¹

(Secondment) The British University in Egypt, Faculty of Engineering, Petroleum and Natural Gas Technology Dept.²

Abstract: Bubble point pressure is an important reservoir fluid property. Many reservoir engineering calculations are bubble point pressure dependable, such as reserve estimation. In circumstances, laboratory PVT analysis is not available, empirical PVT correlations becomes the best alternative. In this study, correlation for bubble point pressure of Egyptian crude oils was developed using non-linear multiple regression. This was done by utilized a total of 178 data points were used to develop this correlation. The data were collected from different fields in Egypt and covered a wide range of crude oils ranging from heavy to volatile oils. The data included oils with bubble point pressures ranging from 180 to 4999 Pisa, °API of 16.5 to 49.8, gas oil ratio of 62 to 2647 scf/STB, gas gravity of 0.6 to 1.474 and temperature of 107 to 316 °F. The developed correlation was taken as a function of solution gas oil ratio, oil API gravity, gas relative density and reservoir temperature. Statistical and graphical analyses have been used to assess the performance of the correlation. Correlation performance was also compared with published correlations. The new correlations developed by this study performed better than existing published bubble point pressure correlations.

Key words: PVT Correlations; Bubble point pressure; Egypt.

I. INTRODUCTION

Reserve estimation, performance prediction and many petroleum engineering calculations in an oil reservoir require demand perfect information of the fluid physical properties. Bubble point pressure is of primary significance in reservoir and production engineering calculation. PVT data can be obtained either by conducting a laboratory study on reservoir fluid samples or estimated by using empirically derived PVT correlations. The accuracy of laboratory results is dependent on the reservoir fluid sample, particularly when the reservoir has depleted below the bubble point pressure. In case where the experimental data are not obtainable, empirically derived correlations are used to estimate the physical reservoir fluid properties. In fact, two different types of correlations in the literature are existing. The first set of correlations is known as worldwide correlations which were developed with selected data sets at random. The second set of correlations was developed with data sets for a specific region in the world or for specific oil. So far there is no general bubble point pressure correlation valid for all types of crude oils over the world. The reason is every crude oil has a unique composition. So the aim of this paper is to evaluate the existing bubble point pressure correlation from the literature and if there is no one valid for Egyptian crude oils, then further modification will be proposed in order to improve the current correlations.

II. LITERATURE REVIEW

The following presents a review of the best-known correlation models published in the literature. Also Table 1 illustrates the literature bubble-point pressure correlations. It shows authors, published year, sample origin, number of data points and the range of bubble point pressure. In 1947, Standing¹ published correlations for p_b and for B_o that were based on laboratory experiments carried out on

105 samples from 22 different crude oils in California, U.S.A. The correlations treated the P_b as a function of the reservoir temperature, GOR, oil gravity, and gas gravity. Actually, these correlations are the most widely used in the oil industry.

In 1958 Lasater² used Henry's law constant and the observation that the bubblepoint ratio at different temperatures is equal to the absolute temperatures ratio for hydrocarbon systems not close to the critical point to develop a p_b correlation. This correlation based on 158 samples from 137 reservoirs in Canada, the U.S., and South America.

In 1980, Vazquez and Beggs³ published correlation for p_b that was based on 6,000 data points from 600 laboratory measurements. They classified oil mixtures into two categories, above 30°API gravity and below 30°API gravity. They also pointed out the strong dependence on gas gravity and developed a correlation to normalize the gas-gravity measurement to a reference separation pressure of 100 psi. This eliminated its dependence on separation conditions.

In 1980 Glaso⁴ presented P_b and other PVT correlations of North Sea hydrocarbon mixtures. The main feature of Glaso's correlations is that they account for paraffinicity by correcting the flash stock-tank-oil gravity to an equivalent corrected value with reservoir temperature and oil viscosity. A total of 45 oil samples, most of which came from the North Sea region, were used in the development of this correlations.

In 1988, Al-Marhoun⁵ published new correlations for estimating p_b and B_o for Middle East oils. A total of 160 data sets from 69 Middle Eastern reservoirs were available for the correlation development.

In 1992, Dokla and Osman⁶ published a new set of correlations for estimating p_b , and B_o for United Arab

Emirates crudes. They used 51 data sets to calculate new coefficients for Al-Marhoun's⁵ 1988 Middle East correlations.

In 1992, Macary and El-Batanony⁷ presented new correlations for Pb, Bo, and GOR. Ninety data sets from 30 independent reservoirs in the Gulf of Suez, Egypt, were used to develop the correlations. The new correlations were tested against other Egyptian data and showed improvement over published correlations.

In 1993 Omar and Todd⁸ developed a Pb correlation that uses the Bo in addition to oil gravity, gas gravity, GOR and reservoir temperature. The new correlation was based on 93 data sets from Malaysian oil reservoirs.

In 1993, Petrosky and Farshad⁹ developed new correlations for Gulf of Mexico crudes. Standing's¹ correlations for Pb, GOR and Bo were taken as the basis for developing the new correlation coefficients.

In 1994, Kartaotmodjo and Schmidt¹⁰ used a global data bank to develop new correlations for all PVT properties. Standing's¹ correlation models were taken as the basis for Pb and GOR correlations. Data from 740 different crude oil samples gathered from all over the world provided 5392 data sets for correlation development.

In 1997, Almehaideb¹¹ published a new set of correlations for UAE crudes. He used 62 data sets from UAE reservoirs to develop the new correlations, for Pb, Bo, oil viscosity, and oil compressibility. The Pb correlation, like Omar and Todd's⁶ uses the Bo as input in addition to oil gravity, gas gravity, GOR and reservoir temperature. Improvement over published correlations was achieved with this work.

In 1997, Hanafy et al. Al.¹² presented new correlations of PVT properties. He used 324 data sets from 75 oil fields distributed along three different regions of Egypt.

In 2001 Al-Shammasi¹³ published correlations and neural-network models for bubblepoint pressure (Pb) and oil formation volume factor (Bo) for their accuracy and flexibility in representing hydrocarbon mixtures from different locations worldwide.

In 1999 Velarde and McCain¹⁴ developed a new bubble-point pressure correlation using the relation proposed by Petrosky⁹ (which is a modification of the original form proposed by Standing¹) using nonlinear regression method.

In 2007 Hemmati and Kharrat¹⁵ used nonlinear regression technique to developed new Pb, Bo and Rs correlations for Iranian crudes using 287 laboratory PVT analyses.

Table 1: literature bubble-point pressure correlations

| Authors | Published year | Sample origin | Number of points | Pb range, Pisa | Reference |
|--------------------------|----------------|----------------|------------------|----------------|-----------|
| Standing | 1947 | California | 105 | 130-7000 | 1 |
| Lasater | 1958 | Canada USA | 158 | 48-5780 | 2 |
| Vazquez and Beggs | 1980 | Worldwide | 6004 | 15-6055 | 3 |
| Glaso | 1980 | North sea | 41 | 165-7142 | 4 |
| Al-Marhoun | 1988 | Middle-East | 160 | 20-3173 | 5 |
| Dokla and Osman | 1992 | U.A.E. | 51 | 590-4640 | 6 |
| Macary and El-Batanony | 1992 | Gulf of Suez | 90 | 1200-4600 | 7 |
| Omar and Todd | 1993 | Malaysia | 93 | 790-3851 | 8 |
| Petrosky and Farshad | 1993 | Gulf of Mexico | 90 | 1574-6523 | 9 |
| Kartaotmodjo and Schmidt | 1994 | Worldwide | 5392 | 15-6055 | 10 |
| Almehaideb | 1997 | U.A.E. | 62 | 501-4822 | 11 |
| Hanafy | 1997 | Egypt | 324 | 36-5003 | 12 |
| Al-Shammasi | 1999 | Worldwide | 1709 | 15-7127 | 13 |
| Velarde and McCain | 1999 | Worldwide | 2097 | 70-6700 | 14 |
| Hemmati and Kharrat | 2007 | Iran | 287 | 348-5156 | 15 |

III. DATA DESCRIPTION

Results of PVT laboratory analyses for Egyptian crude oils constituted the base of information needed for this study. Data used for this work consists of reservoir bubble-point pressure, temperature, oil gravity, gas gravity and solution gas oil ratio. A total of 178 data sets from different fields in Egypt. The data covered a wide range of crude oils ranging from heavy to volatile oils.

Table 2: Data Description of Egyptian Crude Oils

| PVT Property | Minimum | Maximum |
|---------------------------|---------|---------|
| Pb, psi | 180 | 4999 |
| Rs, scf/STB | 62 | 2647 |
| Oil API gravity | 16.5 | 49.8 |
| Gas gravity | 0.6 | 1.474 |
| Reservoir Temperature, °F | 107 | 316 |

Table 2 shows the range of data used in this paper.

IV. CORRELATION DEVELOPMENT

In order to develop a correlation of bubble point pressure of Egyptian crude oils, many models were tried as regression equations to obtain a bubble-point pressure correlation. It was found that, the most familiar one to industry is Standing correlation.

The new black oil correlation was based on Standing's bubble point pressure. The correlation is function of solution gas oil ratio, oil API gravity, gas relative density and reservoir temperature. Based on this correlation, using a nonlinear regression analysis, the best fit and most sensitive coefficient was determined.

The accuracy of the new improved black oil bubble-point pressure correlation was studied by conducting an error analysis (statistical and graphical) and by performing comparative study with other known black oil correlations.

$$Pb = a1 * \left[\left(\frac{RS}{\gamma g} \right)^{a2} * 10^x - a5 \right]$$

$$x = a3 * T - a4 * API$$

$$a1 = 55.67$$

$$a2 = 0.637$$

$$a3 = 0.00045$$

$$a4 = 0.0088$$

$$a5 = 7.957$$

Statistical Error Analysis

There are three main statistical parameters that are being considered in this study. These parameters help to estimate the accuracy of the bubble-point pressure correlations used in this study.

Average Percent Relative Error¹¹ (AE)

This is an indication of the relative deviation in percent from the experimental values and is given as:

$$E_r = \left(\frac{1}{n_d} \right) \sum_{i=1}^{n_d} E_i$$

E_i is the relative deviation in percent of an estimated value from an experimental value and is defined by

$$E_i = \left[\frac{(x_{est} - x_{exp})}{x_{exp}} \right]_i \times 100, \quad i = 1, 2, \dots, n_d$$

Where X_{est} and X_{exp} represent the estimated and experimental values, respectively. The lower the value of E_r , the more equally distributed is the errors between positive and negative values.

Average Absolute Percent Relative Error¹¹ (AAE)

This parameter is to measure the average value of the absolute relative deviation of the measured value from the experimental data. The value of AAE is expressed in percent. The parameter can be defined as

$$E_a = \left(\frac{1}{n_d} \right) \sum_{i=1}^{n_d} |E_i|$$

This parameter indicates the relative absolute deviation in percent from the experimental values. A lower value of AAE implies better agreement between the estimated and experimental values.

Correlation Coefficient¹¹

The objective of performing correlation coefficient calculation is to characterize the extent of the connection between two variables namely experimental and estimated values obtained from the correlation.

The value of the correlation coefficient varies from -1.0 to +1. A coefficient of zero indicates no relationship between experimental and calculated values. A +1.0 coefficient indicates a perfect positive relationship and a -1.0 coefficient indicates a perfect negative relationship. The correlation coefficient can be determined using the following equation:

$$r^2 = 1 - \frac{\sum_{i=1}^m [(x_{exp} - x_{est})_i]^2}{\sum_{i=1}^m [(x_{exp} - \bar{x})_i]^2}$$

where

$$\bar{x} = \left(\frac{1}{n_d} \right) \sum_{i=1}^{n_d} (x_{exp})_i$$

Graphic Error Analysis¹¹

Graphic means assist in visualizing the accuracy of a correlation. One graphic analysis technique was used in this paper.

Cross plot

In this method, all the predicted values are plotted versus the experimental values and thus cross plot is formed. A 45° straight line is drawn on the cross plot on which the estimated value is equal to the experimental value. The closer the plotted data points are to this line, better the correlation.

V. RESULT AND DISCUSSION

The average percent relative error, average absolute percent, correlation coefficient and were computed for each correlation. Also cross plot is drawn for each correlation.

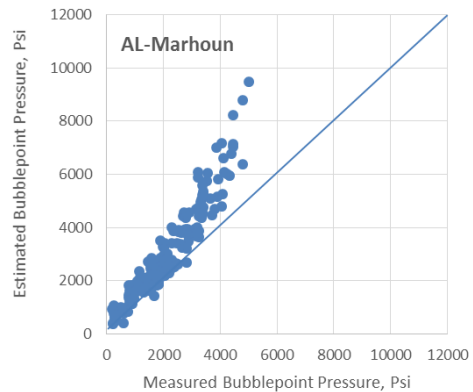
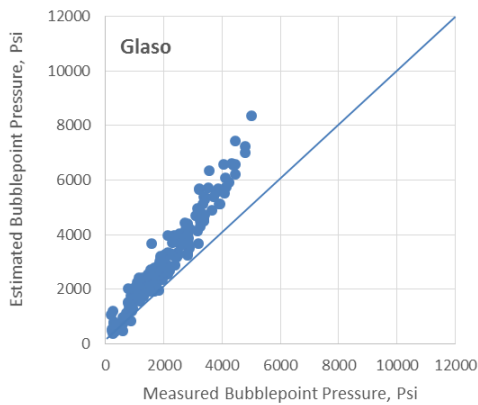
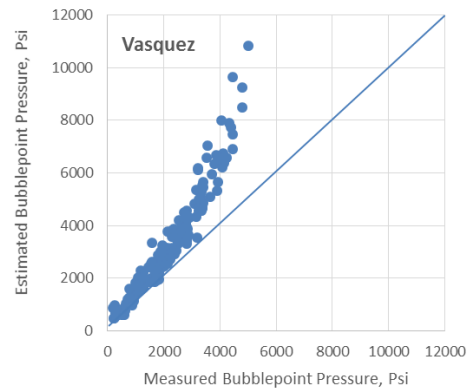
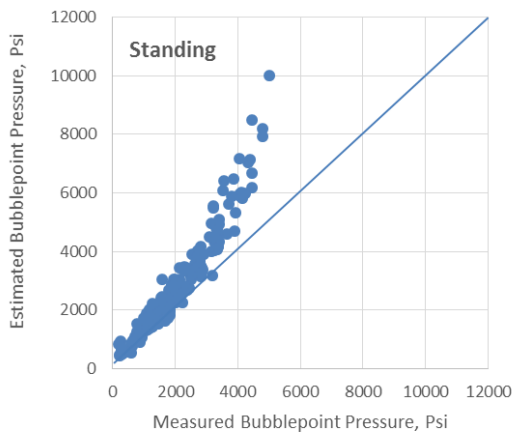
Table 3 illustrates the results of statistical error analysis of the developed bubble-point pressure correlation in this study and for the other Literature correlations.

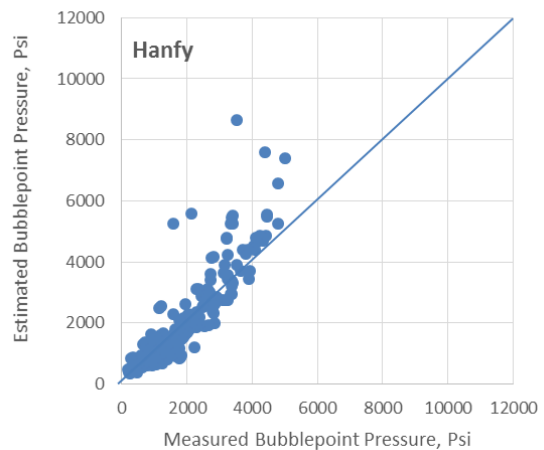
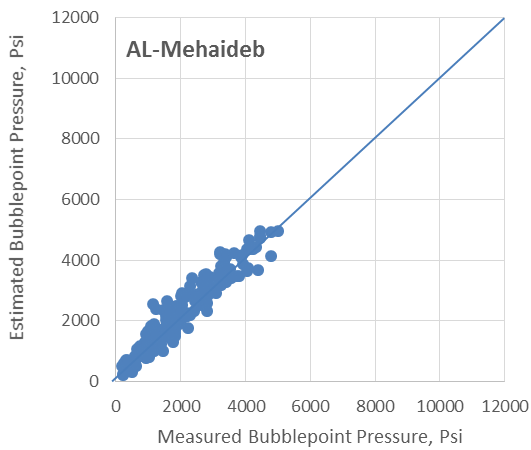
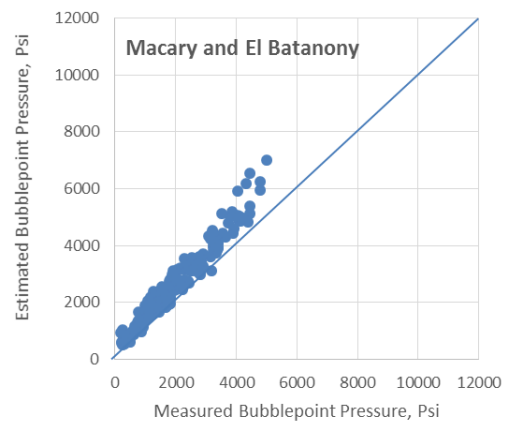
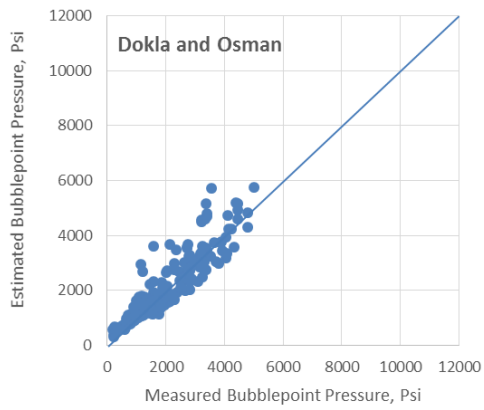
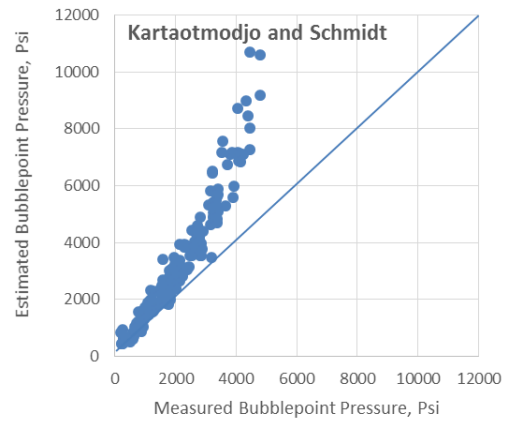
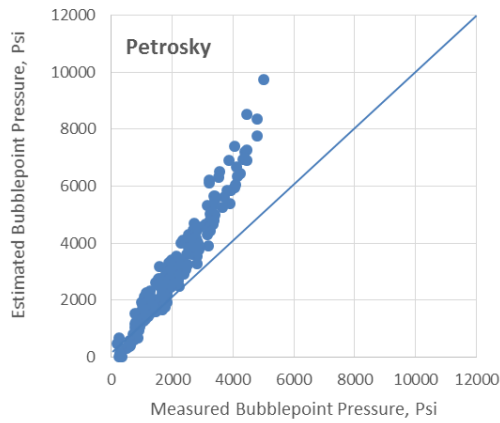
The bubble-point pressure correlation gives low values of average percent relative error (AE %), absolute average percent relative error (AAE %) and high value of correlation coefficient of 1.15 percent, 13.6 percent and 0.95 respectively. A lower value of these statistical error analysis variables indicates a better accuracy of the correlation. The correlation coefficient shows that a good agreement exists between experimental and calculated bubble point pressure.

In comparison with other known correlations, the developed one in this paper gives the lowest AE % and AAE %. This shows that this correlation predicts better bubble point pressure for Egyptian crude oils than any other known correlations. The cross plot of the experimental against the calculated bubble point pressure using the new correlation and all the other correlations used in this study is presented in Figure 1. Most of the data points of the new correlation fall very close to perfect correlation of the 45° line.

Table 3: Statistical Error Analysis

| Bubble-point Pressure Correlations | AE% | AAE% | R ² |
|------------------------------------|--------|-------|----------------|
| Standing | -43.8 | 43.9 | Negative |
| Lasater | -106.9 | 106.9 | Negative |
| Vasquez and Beggs | -55.7 | 55.7 | Negative |
| Glaso | -60.1 | 60.3 | Negative |
| AL-Marhoun | -52.6 | 53.2 | 0.724 |
| Dokla and Osman | -13.1 | 24.4 | 0.772 |
| Macary and EL-Batanony | -42.6 | 43.1 | 0.62 |
| Omar and Todd | -45.5 | 45.5 | 0.52 |
| Petrosky and Farshad | -39.6 | 52.8 | Negative |
| Kartaotmodjo and Schmidt | -57.6 | 57.6 | Negative |
| Al-Mehaideb | -17.3 | 22.2 | 0.863 |
| Hanafy | -11.6 | 29.6 | 0.46 |
| AL-Shammasi | -43.1 | 43.1 | 0.36 |
| Velarde and McCain | -43.7 | 44.2 | 0.36 |
| Hemmati and Kharrat | -31.2 | 32.4 | 0.393 |
| This study | 1.15 | 13.6 | 95 |





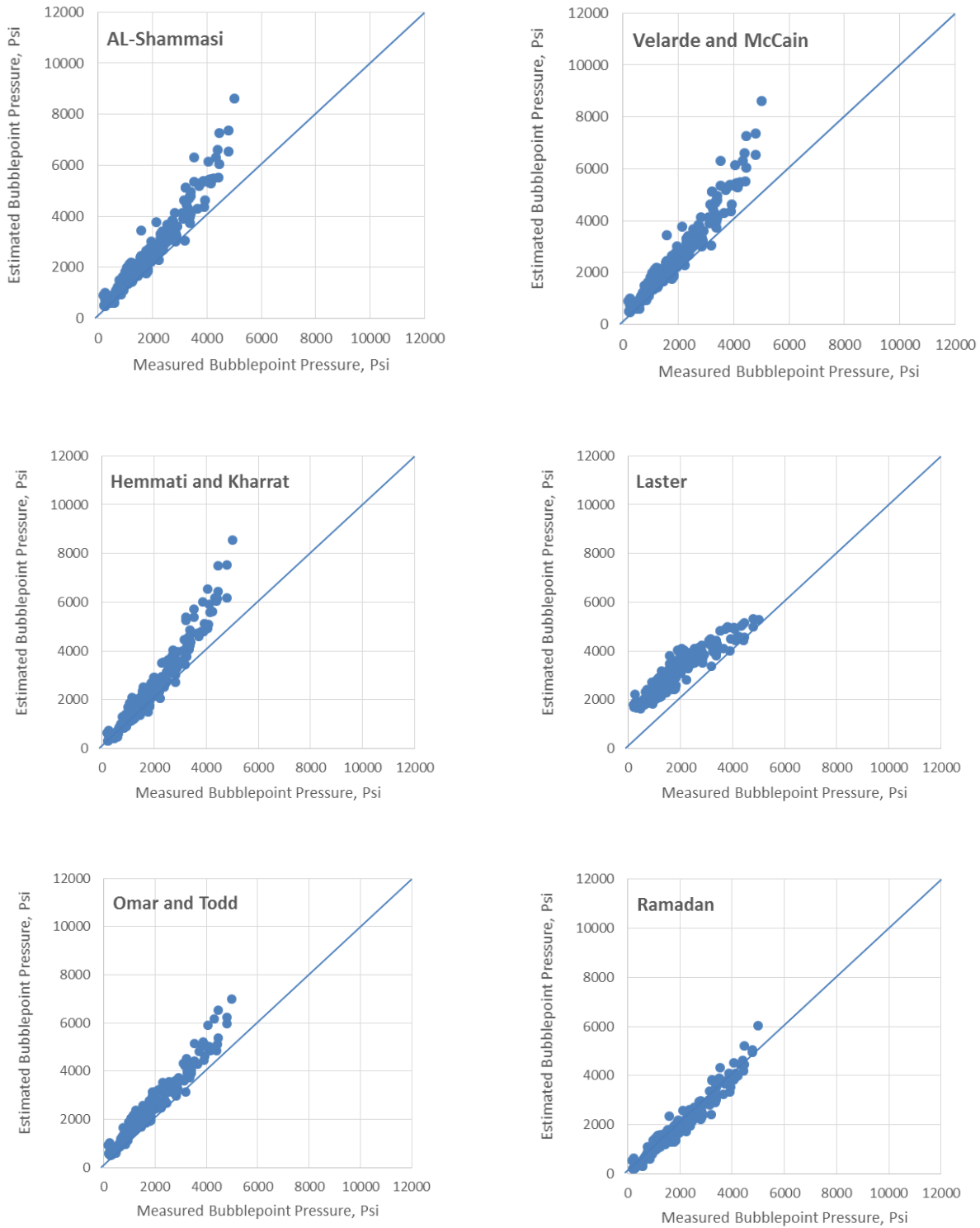


Fig 1: Cross Plot for the Evaluated Pb Correlation

VI. CONCLUSION

New bubble-point pressure correlation was obtained for Egyptian crudes using nonlinear regression technique. This correlation was developed based on Standing's correlation. The new correlations gave better accuracy in estimating bubble-point pressure of Egyptian crudes as compared with other known correlations available in the literature. The new correlation was developed specifically for Egyptian crude oils but can be used for estimating the same bubble-point pressure for all types of oil and gas mixtures with properties falling within the range of the data used in this study. The bubble-point pressure correlations can be placed in the following order with respect to their accuracy: a) This study, Al-Mehaideb, Dokla and Osman, and Hanafy.

NOMENCLATURE:

E_i = Percent relative error

E_r = Average relative error

E_a = Average absolute relative error, %

n_d = Number of data points

P_b = Bubble point Pressure, psia

B_o = oil formation volume factor, bbl/STB

T = Temperature, oF

r = Coefficient of correlation

R_s = Solution gas-oil-ratio, scf/STB

x = Any physical quantity

\bar{x} = Average value of X

γ_g = Gas specific gravity

SUBSCRIPTS:

b= bubble point

est =estimated from correlation

exp = experimental

g= gas

o= oil

s = solution

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