

Hybrid technique for MHD free convection flow and heat transfer of Nano-fluid

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Abstract: A numerical model is created for the nanofluid stream and warmth move because of the imprudent movement of an endless vertical permeable plate in its own plane within the sight of an attractive field and gooey dissemination. The overseeing flimsy, coupled, nonlinear incomplete differential conditions are changed into an arrangement of nonlinear standard differential conditions, with suitable limit conditions. A powerful Galerkin limited component mathematical arrangement is created. A [1]scope of nanofluids containing nanoparticles of aluminum oxide, copper, titanium oxide and silver with nanoparticle volume division goes not exactly or equivalent to 0.04 are thought of. The Tiwari-Das nanofluid model is utilized. The [2]speed and temperature profiles just as the skin grating coefficient and Nusselt number are inspected for various boundaries, for example, nanoparticle volume part, nanofluid type, attractive boundary, warm Grashof number, Eckert number and pull boundary. The current reproductions are applicable to attractive nanomaterials warm stream preparing in the synthetic designing and metallurgy ventures.

Keywords—Nanofluid , Galerkin , copper ,numerical model ,metallurgy.

1. INTRODUCTION

Nomenclature	
M	Magnetic parameter
Ec	Eckert number
λ	suction parameter
Gr	thermal Grashof number
t	time
T	temperature
U	velocity along x-axis,
ρ	density
μ	dynamic viscosity
β	thermal expansion coefficient
g	acceleration due to gravity,
κ	thermal conductivity
n	empirical shape factor for the nanoparticle
ϕ	nanoparticle volume fraction
ν	kinematic viscosity
subscripts	
nf	nanofluids
f	base fluid
s	solid nanoparticles

Convictional heat move liquids, including oil, water, and ethylene glycol blend are helpless warmth move fluids. Since [3]the warmth conductivity of these liquids assumes a significant part in deciding the coefficient of warmth move between the warmth move medium and the warmth move surface, various techniques [4]have been utilized to improve the warmth conductivity of these liquids by suspending nanometre/micrometer-sized molecule materials in liquids. Intensive consideration has been aimed at mathematical reproductions of normal convection heat move in nanofluids both with and without attractive fields, and delegate examines incorporate [5]Congedo et al.(2009). Uddin et al.(2014) utilized MAPLE emblematic quadrature to concentrate mathematically the electromagnetic nanofluid stream in permeable media with divider slip [6]and radiation heat move impacts. Bég et al.(2014) applied understood limited contrast techniques to dissect the attractive bio-nanofluid acceptance stream from an extending surface with surface strain impacts. Rana et al. (2013) utilized a variation limited component [7]technique to mimic pivoting attractive nanofluid limit layer stream, warmth and mass exchange from an expelling sheet. As of late Rajesh et al.(2014) introduced a numerical model for the flimsy free convective stream and warmth move of a thick nanofluid from a moving vertical chamber within the sight of warmth radiation. Later Rajesh and Anwar Beg (2014) mathematically examined the impacts of MHD on the transient free convection stream of a gooey, electrically leading, and incompressible nanofluid past a moving semi-limitless



vertical chamber with temperature oscillation. Transient free [8] convection streams affected by an attractive field have drawn in light of a legitimate concern for some specialists considering their applications in present day materials preparing where attractive fields are known to accomplish great control and control of electrically-directing materials (Ibrahim and Shankar, 014). Magneto hydrodynamic (MHD) convection streams likewise discover huge applications in environmentally friendly power devices, including MHD power generators (Chen et. al.2005, Yamaguchi, 2011) just as atomic reactor transport measures (Mukhopadhyay, 2011) wherein attractive field is utilized to direct warmth move rates. Taking into account these applications, [9] the current investigation is proposed to analyze the impacts of cross over attractive field on transient free convective progression of nanofluid past an imprudently begun limitless vertical permeable plate with thick scattering. The [10] present investigation additionally gives a significant benchmark to additional re-enactments of magneto-nanofluid dynamic vehicle marvels of importance to materials preparing, with elective computational calculations.

2. EXPERIMENTAL METHODS OR METHODOLOGY:

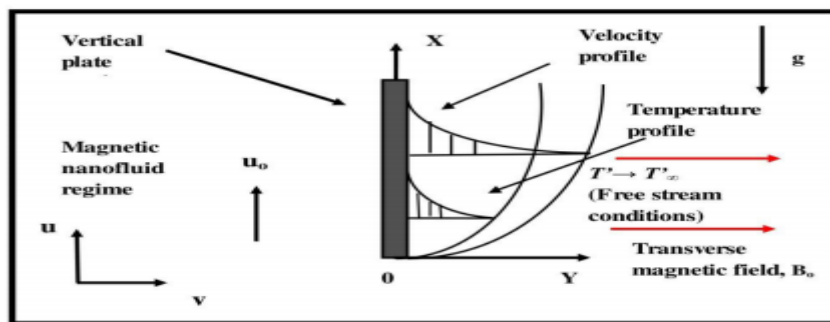


Figure 1: The physical model and coordinate system

$$\frac{\partial v}{\partial y} = 0 \tag{1}$$

$$\frac{\partial u}{\partial t'} + v \frac{\partial u}{\partial y} = \nu_{nf} \frac{\partial^2 u}{\partial y^2} + \frac{(\rho\beta)_{nf}}{\rho_{nf}} g(T' - T'_\infty) - \frac{\sigma B_0^2 u}{\rho_{nf}} \tag{2}$$



$$\frac{\partial T'}{\partial t'} + v \frac{\partial T'}{\partial y} = \frac{\kappa_{nf}}{(\rho c_p)_{nf}} \frac{\partial^2 T'}{\partial y^2} + \frac{\mu_{nf}}{(\rho c_p)_{nf}} \left(\frac{\partial u}{\partial y} \right)^2 \quad (3)$$

The initial and boundary conditions are

$$\begin{aligned} t' \leq 0: & \quad u=0, \quad T'=T'_\infty \quad \text{for all } y \\ t' > 0: & \quad u = u_0, \quad T' = T'_w \quad \text{for } y=0 \\ & \quad u \rightarrow 0, \quad T' \rightarrow T'_\infty \quad \text{as } y \rightarrow \infty \end{aligned} \quad (4)$$

$$\text{Equation (1) gives} \quad v = -v_0 \quad (v_0 > 0) \quad (5)$$

Where v_0 is the constant suction velocity and the negative sign indicates that it is towards the plate.

For nanofluids, the expressions of density ρ_{nf} , thermal expansion coefficient $(\rho\beta)_{nf}$ and heat capacitance $(\rho c_p)_{nf}$ are given by

$$\begin{aligned} \rho_{nf} &= (1-\phi)\rho_f + \phi\rho_s \\ (\rho\beta)_{nf} &= (1-\phi)(\rho\beta)_f + \phi(\rho\beta)_s \\ (\rho c_p)_{nf} &= (1-\phi)(\rho c_p)_f + \phi(\rho c_p)_s \end{aligned} \quad (6)$$

The effective thermal conductivity of the nanofluid according to Hamilton and Crosser (1962) model is given by

$$\frac{\kappa_{eff}}{\kappa_f} = \frac{\kappa_s + (n-1)\kappa_f - (n-1)\phi(\kappa_f - \kappa_s)}{\kappa_s + (n-1)\kappa_f + \phi(\kappa_f - \kappa_s)} \quad (7)$$

Where n is the empirical shape factor for the nanoparticle. In particular, $n=3$ for spherical shaped nanoparticles and $n=3/2$ for cylindrical ones.

Table 1. Thermo-physical properties of water and nanoparticles

	H_2O	Al_2O_3	Cu	TiO_2	Ag
$\rho (Kg m^{-3})$	997.1	3970	8933	4250	10500
$C_p (J Kg^{-1} K^{-1})$	4179	765	385	686.2	235
$\kappa (Wm^{-1} K^{-1})$	0.613	40	401	8.9528	429
$\beta \times 10^{-5} (K^{-1})$	21	0.85	1.67	0.9	1.89

Introducing the following non dimensional variables in equations (2) and (3):

$$U = \frac{u}{u_0}, \quad t = \frac{t' u_0^2}{v_f}, \quad Y = \frac{y u_0}{v_f}, \quad T = \frac{T' - T'_\infty}{T'_w - T'_\infty}, \quad G_r = \frac{g \beta_f v_f (T'_w - T'_\infty)}{u_0^3}, \quad P_r = \frac{v_f}{\alpha_f} = \frac{(\mu c_p)_f}{k_f},$$

$$M = \frac{\sigma B_0^2 v_f}{\rho_f u_0^2}, \lambda = -\frac{v}{u_0}, E_c = \frac{u_0^2}{(c_p)_f (T_w - T_\infty)} \tag{8}$$

The governing equations reduces to

$$\frac{\partial U}{\partial t} - \lambda \frac{\partial U}{\partial Y} = \frac{1}{(1-\phi)^{2.5}} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho_s}{\rho_f}\right)\right)} \frac{\partial^2 U}{\partial Y^2} + \frac{\left(1-\phi + \phi \left(\frac{\rho\beta}{\rho\beta}_f\right)\right)}{\left(1-\phi + \phi \left(\frac{\rho}{\rho}_f\right)\right)} GrT - \frac{1}{\left(1-\phi + \phi \left(\frac{\rho_s}{\rho_f}\right)\right)} MU \tag{9}$$

$$\frac{\partial T}{\partial t} - \lambda \frac{\partial T}{\partial Y} = \frac{k_{nf}}{k_f} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho c_p}{\rho c_p}_f\right)\right)} \frac{1}{P_r} \frac{\partial^2 T}{\partial Y^2} + \frac{1}{(1-\phi)^{2.5}} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho c_p}{\rho c_p}_f\right)\right)} E_c \left(\frac{\partial U}{\partial Y}\right)^2 \tag{10}$$

The corresponding dimensionless boundary conditions are:

$$\begin{aligned} t \leq 0: U=0, \quad T=0 \quad \text{for all } Y \\ t > 0: U=1, \quad T=1 \quad \text{at } Y=0 \\ U \rightarrow 0, \quad T \rightarrow 0 \quad \text{as } Y \rightarrow \infty \end{aligned} \tag{11}$$

$$\text{Let } E_1 = \frac{1}{(1-\phi)^{2.5}} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho_s}{\rho_f}\right)\right)}, E_2 = \frac{\left(1-\phi + \phi \left(\frac{\rho\beta}{\rho\beta}_f\right)\right)}{\left(1-\phi + \phi \left(\frac{\rho}{\rho}_f\right)\right)}, E_3 = \frac{1}{\left(1-\phi + \phi \left(\frac{\rho_s}{\rho_f}\right)\right)},$$

$$E_4 = \frac{k_{nf}}{k_f} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho c_p}{\rho c_p}_f\right)\right)}, E_5 = \frac{1}{(1-\phi)^{2.5}} \frac{1}{\left(1-\phi + \phi \left(\frac{\rho c_p}{\rho c_p}_f\right)\right)}$$

Now the equations (8) and (10) in terms of E_1, E_2, E_3, E_4 and E_5 are

$$\frac{\partial U}{\partial t} - \lambda \frac{\partial U}{\partial Y} = E_1 \frac{\partial^2 U}{\partial Y^2} + E_2 GrT - E_3 MU \tag{12}$$

$$\frac{\partial T}{\partial t} - \lambda \frac{\partial T}{\partial Y} = E_4 \frac{1}{P_r} \frac{\partial^2 T}{\partial Y^2} + E_c E_5 \left(\frac{\partial U}{\partial Y}\right)^2 \tag{13}$$

3. SOLUTION

$$\int_{Y_j}^{Y_k} N^{(e)T} \left(E_1 \frac{\partial^2 U^{(e)}}{\partial Y^2} + \lambda \frac{\partial U^{(e)}}{\partial Y} - \frac{\partial U^{(e)}}{\partial t} + E_2 GrT - E_3 MU^{(e)} \right) dY = 0 \tag{14}$$

$$\int_{Y_j}^{Y_k} N^{(e)T} \left(E_4 \frac{1}{Pr} \frac{\partial^2 T^{(e)}}{\partial Y^2} + \lambda \frac{\partial T^{(e)}}{\partial Y} - \frac{\partial T^{(e)}}{\partial t} + E_c E_5 \left(\frac{\partial U}{\partial Y} \right)^2 \right) dY = 0 \tag{15}$$

Let the linear, piecewise approximation solution be

$$U^e = N_j(Y)U_j(t) + N_k(Y)U_k(t) = N_j U_j + N_k U_k \tag{16}$$

$$T^e = N_j(Y)T_j(t) + N_k(Y)T_k(t) = N_j T_j + N_k T_k \tag{17}$$

Where

$$N_j = \frac{Y_k - Y}{Y_k - Y_j}, N_k = \frac{Y - Y_j}{Y_k - Y_j}, N^{(e)T} = [N_j \ N_k]^T = \begin{bmatrix} N_j \\ N_k \end{bmatrix} \tag{18}$$

Table 2. Thermal conductivity and dynamic viscosity for spherical shaped nanoparticles

Model	Shape of nanoparticles	Thermal conductivity	Dynamic viscosity
I	Spherical	$\frac{\kappa_{nf}}{\kappa_f} = \frac{\kappa_s + 2\kappa_f - 2\phi(\kappa_f - \kappa_s)}{\kappa_s + 2\kappa_f + \phi(\kappa_f - \kappa_s)}$	$\mu_{nf} = \frac{\mu_f}{(1-\phi)^{2.5}}$
II	Spherical	$\frac{\kappa_{nf}}{\kappa_f} = \frac{\kappa_s + 2\kappa_f - 2\phi(\kappa_f - \kappa_s)}{\kappa_s + 2\kappa_f + \phi(\kappa_f - \kappa_s)}$	$\mu_{nf} = \mu_f (1 + 7.3\phi + 123\phi^2)$

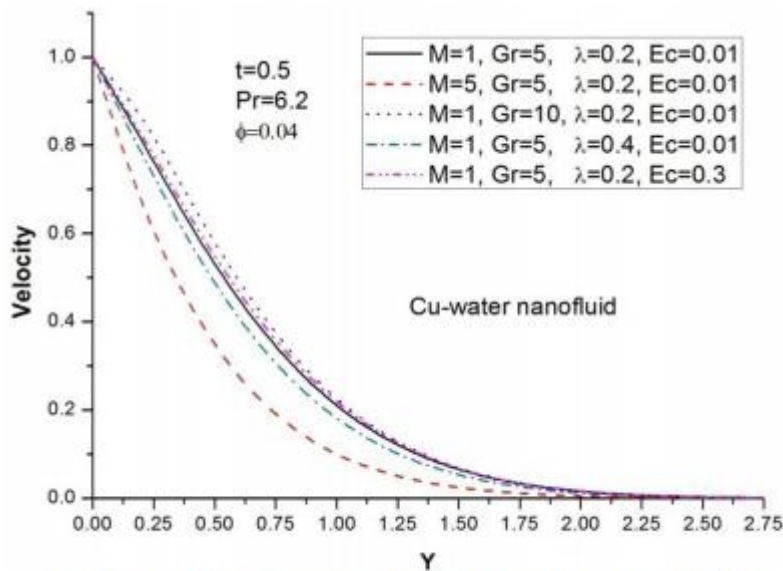


Figure 2. Transient velocity profiles for different M, Gr, Ec, λ

4. RESULTS AND DISCUSSIONS:

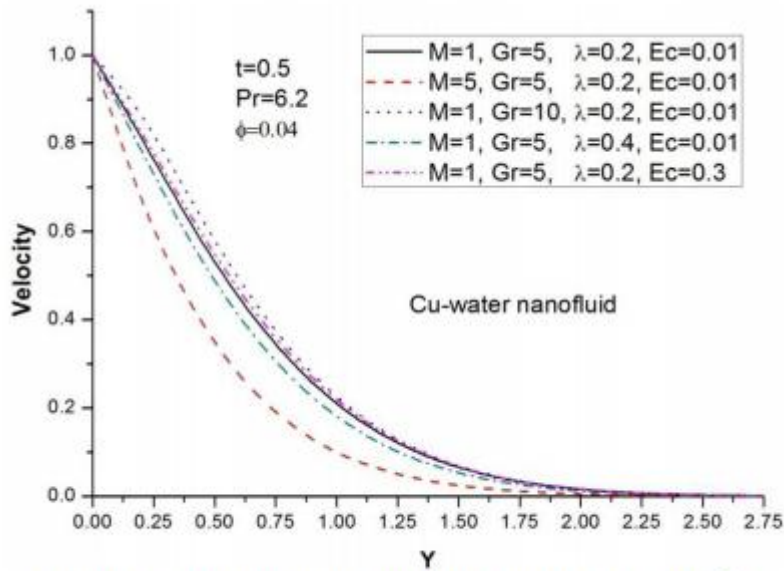


Figure 2. Transient velocity profiles for different M, Gr, Ec, λ

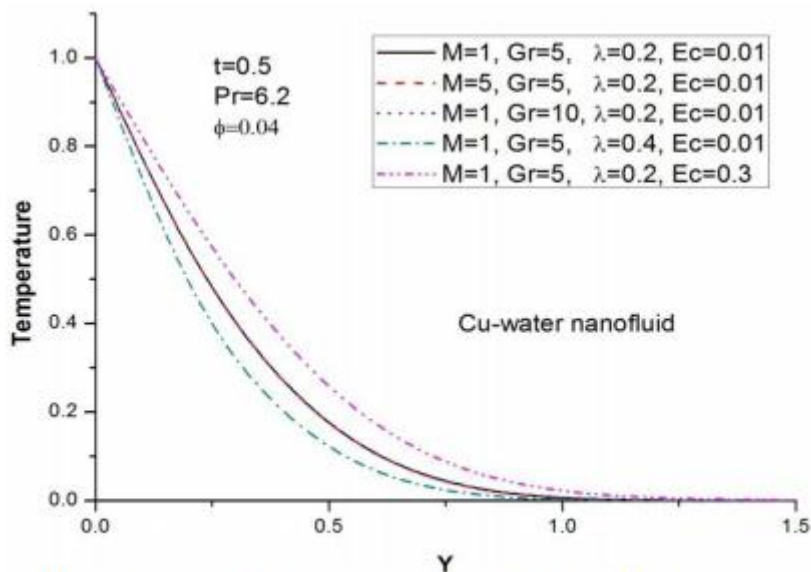


Figure 3. Transient temperature profiles for different M, Gr, Ec, λ

Table 3. Transient velocity of Cu-water nanofluid for different ϕ and t

Y	t=0.5			t=1		
	$\phi = 0$	$\phi = 0.02$	$\phi = 0.04$	$\phi = 0$	$\phi = 0.02$	$\phi = 0.04$
0	1	1	1	1	1	1
0.4	0.6376	0.6286	0.6209	0.7288	0.7252	0.7219
0.8	0.3391	0.3256	0.3145	0.4587	0.4533	0.4486
1	0.2363	0.2224	0.211	0.3521	0.3456	0.3401
1.4	0.1056	0.0941	0.0851	0.1987	0.191	0.1845
1.8	0.0417	0.0346	0.0293	0.107	0.0997	0.0937
2	0.0249	0.0197	0.0161	0.0772	0.0705	0.0651
2.4	0.0079	0.0057	0.0042	0.0386	0.0337	0.0299
2.8	0.0022	0.0013	0.0009	0.0182	0.0151	0.0127
3	0.0011	0.0006	0.0004	0.0122	0.0098	0.0081
3.4	0.0002	0.0001	0.0001	0.0053	0.0039	0.003
3.8	0	0	0	0.0021	0.0014	0.001
4	0	0	0	0.0013	0.0009	0.0006

CONCLUSION

This paper explored transient MHD free convection stream and warmth move of nanofluid past an imprudently begun vertical permeable plate within the sight of gooey scattering. Mathematical computations are done for different upsides of the dimensionless boundaries. The impacts of different actual boundaries on the nanofluid stream and warmth move attributes were inspected. The current calculations have shown that the pace of warmth move diminished with the expansion in Magnetic boundary and Eckert number. In any case, as Suction boundary and nanoparticle volume part expanded, the pace of warmth move expanded for all nanofluids. Picking copper as nanoparticle prompts the improved warmth move rate contrasted with the other nanofluids.

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